

# KAOS project

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June 14, 2016

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# Agenda

Topics covered (in isolation) relevant for the KAOS project

- Prediction of completion time of process instances
- Online mining of event streams

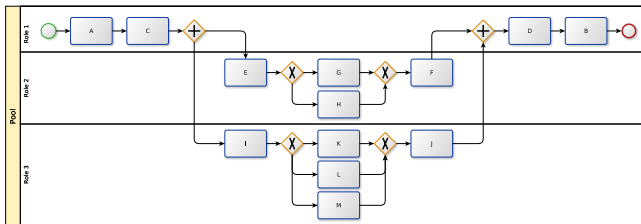
In KAOS, our goal is to “merge” these two aspects

# Chapter 1

Prediction of completion time of process instances

# Business Processes

- Set of tasks or activities
- Set of dependencies among activities
- The execution of an activity corresponding to a process task triggers an event logging on one or more information systems



# Event log

Ev.#	Basic data		Additional data		
	Activity	Time	Resource	Cost	...
<b>Case Id: <math>C_1</math></b>					
1	A	2016-01-01	John	75	...
2	B	2016-01-02	John	5	...
3	C	2016-01-03	Joe	7	...
4	E	2016-01-04	John	1	...
<b>Case Id: <math>C_2</math></b>					
1	A	2016-01-02	Jack	65	...
2	B	2016-01-03	Joe	8	...
3	D	2016-01-04	John	7	...
4	E	2016-01-05	Jack	10	...

# Remaining Time Prediction

## Goal

Given a partial trace (i.e. running process instance), we want to predict the remaining time (i.e. time to complete).

## Strong Business Motivations

- Avoid SLAs violations
- Take precautions if cases seem to take too much time
- Good waiting time estimation for customers

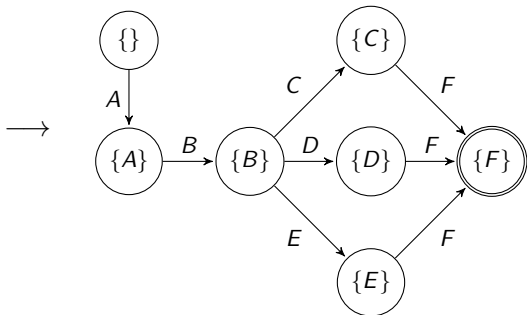
# State of the art

*Time Prediction Based on Process Mining,*  
van der Aalst et al. (2011)

Steps:

1. Creation of a transition system
2. Transition system annotation with statistical information

$\langle A^0, B^4, C^{10}, F^{15} \rangle$   
 $\langle A^0, B^6, D^{13}, F^{15} \rangle$   
 $\langle A^0, B^7, E^9, F^{16} \rangle$   
 $\langle A^0, B^2, C^{15}, F^{19} \rangle$   
 $\langle A^0, B^{11}, D^{13}, F^{14} \rangle$   
 $\langle A^0, B^6, E^9, F^{12} \rangle$   
...



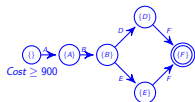
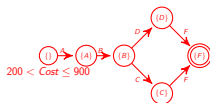
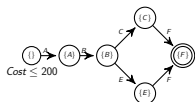
# State of the art (cont.)

*Discovering High-Level Performance Models for Ticket Resolution Processes*, Folino et al. (2013)

Steps:

1. Traces clustering (*Clustering Tree*)
2. van der Aalst et al. approach on each cluster

$\langle A^0, B^4, C^{10}, F^{15} \rangle$ , Cost = 100  
 $\langle A^0, B^6, D^{13}, F^{15} \rangle$ , Cost = 500  
 $\langle A^0, B^7, E^9, F^{16} \rangle$ , Cost = 600  
 $\langle A^0, B^2, C^{15}, F^{19} \rangle$ , Cost = 1000  
 $\langle A^0, B^{11}, D^{13}, F^{14} \rangle$ , Cost = 200  
 $\langle A^0, B^6, E^9, F^{12} \rangle$ , Cost = 900  
...





# Prediction framework overview

## Idea

Using additional data attributes in the event log in order to improve the prediction quality:

- Estimate the likelihood of the next activity
  - Estimate the remaining time
- 
- Exploit the idea in “*Time prediction based on Process Mining*” (2011)
  - Consider additional data attributes
  - Application of Machine Learning techniques
    - Naïve Bayes (NB) classifier
    - Support Vector Regressor (SVR)

# Transition System (TS)

<b>Id</b>	<b>Case Id</b>	<b>Timestamp</b>	<b>Activity</b>	<b>Resource</b>	<b>Cost</b>	<b>...</b>
e <sub>5</sub>	2	19-02-2016:09.10	A	Jack	200	
e <sub>6</sub>	2	19-02-2016:13.22	B	John	200	
e <sub>7</sub>	2	10-02-2016:17.17	D	John	200	
e <sub>8</sub>	2	21-02-2016:10.38	F	Joe	200	

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- Event representation function  $f^{event}$ . E.g.,  $f^{event}(e_5) = A$

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- State representation function  $f^{state}$ . E.g :
  - $f_{set^1}^{state}(\langle A, B, D, F \rangle) = \{F\}$
  - $f_{set^\infty}^{state}(\langle A, A, B, D, F \rangle) = \{A, B, D, F\}$
  - $f_{list^\infty}^{state}(\langle A, B, D, F \rangle) = \langle A, B, D, F \rangle$

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- $f^{event}$  and  $f^{state}$  are *abstraction*

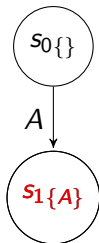
# TS Construction

$$\sigma_1 = \langle A, B, C, F \rangle$$



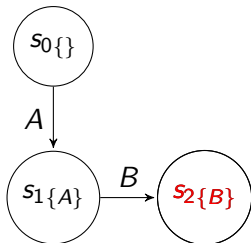
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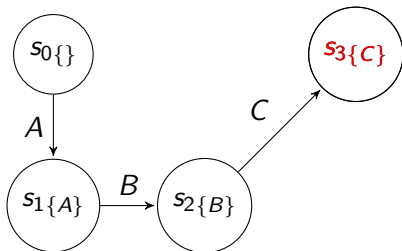
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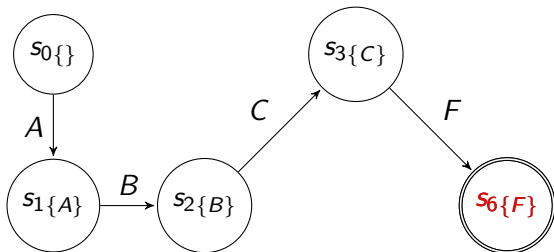
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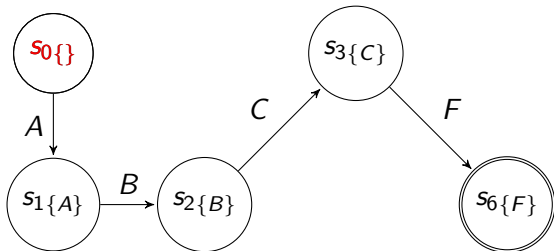
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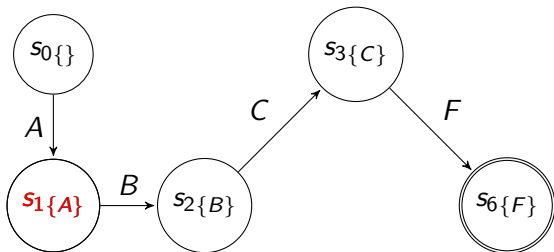
# TS Construction

$$\sigma_2 = \langle A, B, D, F \rangle$$



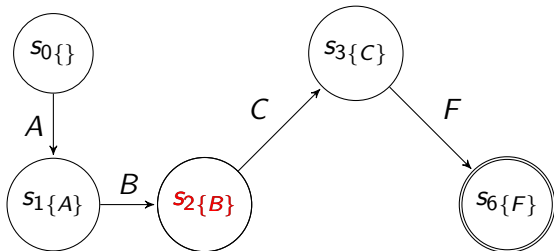
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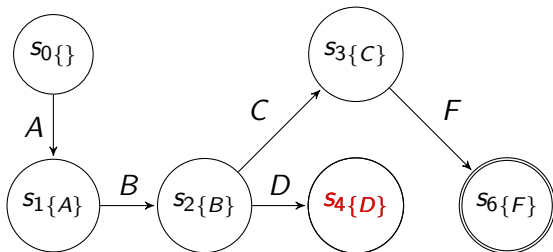
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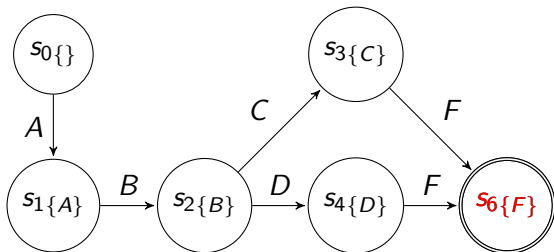
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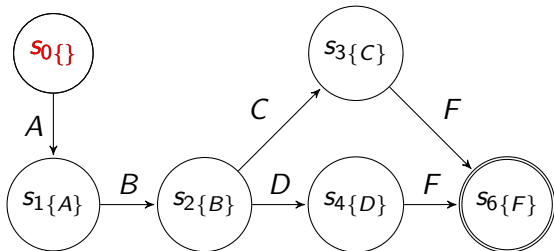
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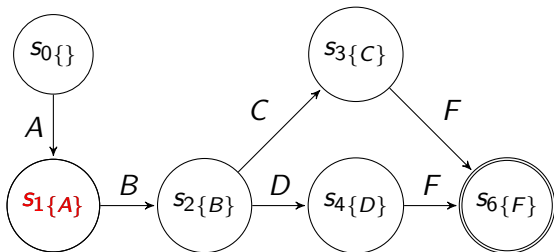
$$\sigma_3 = \langle A, B, E, F \rangle$$





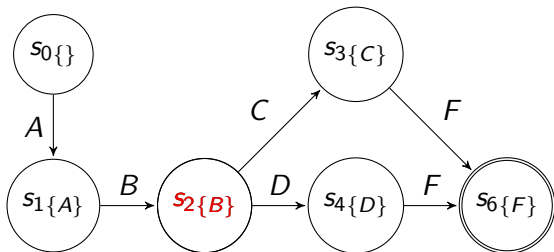
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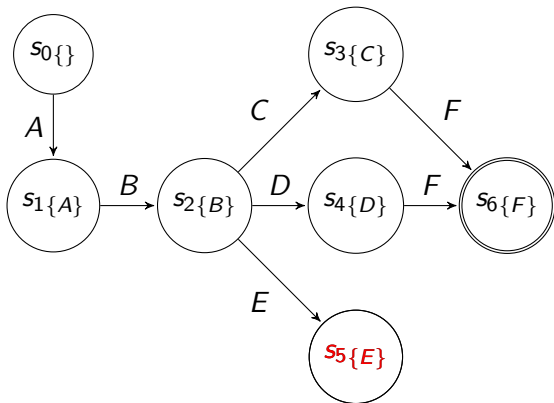
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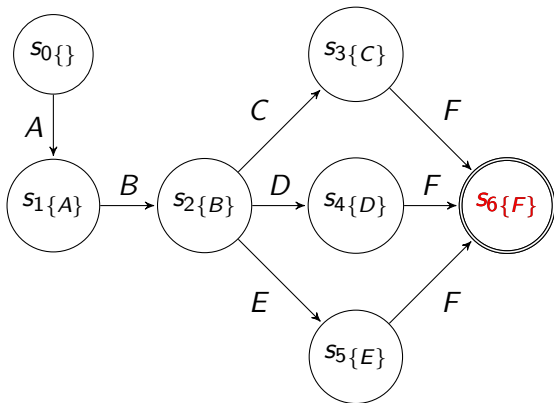
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# Training examples

Id	Case Id	Timestamp	Activity	Resource	Cost	...
$e_5$	2	19-02-2016:09.10	A	Jack	200	...
$e_6$	2	19-02-2016:13.22	B	John	200	...
$e_7$	2	10-02-2016:17.17	D	John	200	...
$e_8$	2	21-02-2016:10.38	F	Joe	200	...

- One-Hot encoding for literal attributes, e.g.,  
 $\text{Res} \in \{Jack, John, Joe\}$ ;  $Jack = [1, 0, 0]$ ;  $John = [0, 1, 0]$ , ...

- Naïve Bayes training example for state  $s_2$

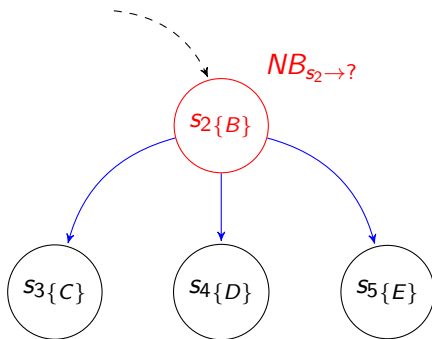
$e_7^{Activity}$	Resource	Cost	...
D	0 1 0	200	...

- SVR training example for transition  $s_2 \rightarrow s_4$

$e_8^{time} - e_6^{time}$	Resource	Cost	...
162960	0 1 0	200	...

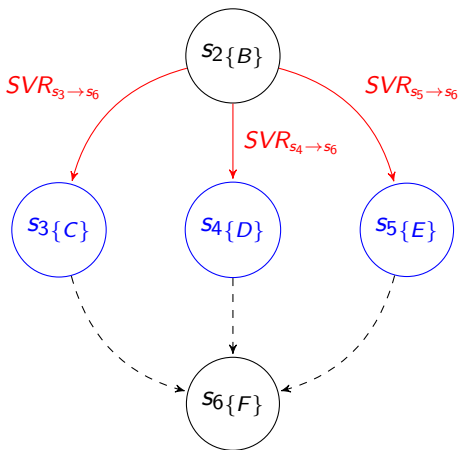
# State Annotations

Naïve Bayes Classifier estimates the likelihood of the next activity



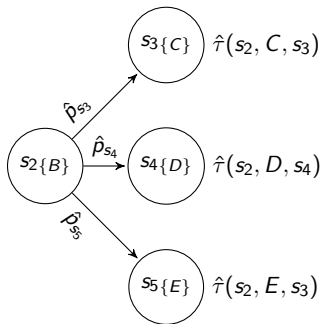
# Transition Annotations

SVR estimates the remaining time starting from the target state of the transition



# Prediction

Given a partial trace  $\sigma$  s.t.  $f^{state}(\sigma) = s_2$

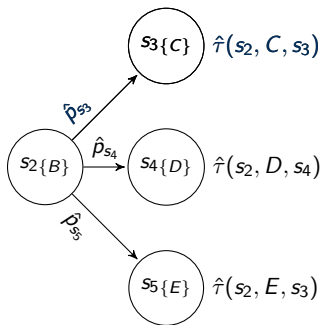


$$prediction(\sigma) = \sum_{(s_2, e, s') \in T_{s_2}} \hat{p}_{s'} \cdot \hat{\tau}(s_2, e, s')$$



# Prediction

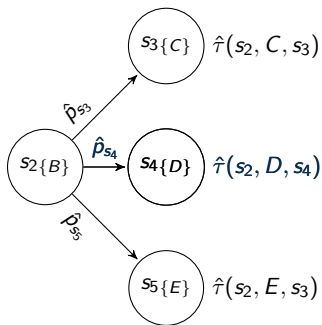
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# Prediction

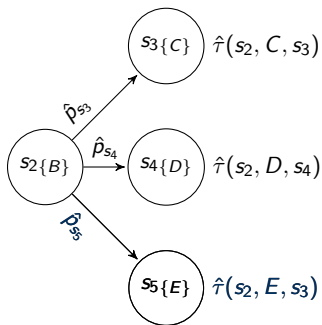
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# Experimental settings

- Implementation in ProM 6 (Java)
- Weka as machine learning module
- 5-cross fold validation
- Road-traffic fines log
- SVR ( $C = 1$ ) kernels
  - RBF with  $\gamma = 10$
  - Polynomial with degree = 3

How we measure error ( $A$ : actual;  $F$ : predicted):

- $\frac{100\%}{n} \sum_{i=1}^n \left| \frac{A_i - F_i}{A_i} \right|$  ..... (Mean Absolute Percentage Error)
- $100\% \sqrt{\frac{\sum_{i=1}^n (A_i - F_i)^2}{n}}$  ..... (Root Mean Square Prediction Error)

# Results

	Our Approach				van der Aalst et al.	
Abs.	Polynomial Kernel		RBF Kernel		MAPE	RMSPE
	MAPE	RMSPE	MAPE	RMSPE		
<b>Event Log with 1500 Traces</b>						
Set 1	<b>8.93%</b>	<b>2.69%</b>	9.13%	2.73%	23.04%	3.53%
Set $\infty$	7.61%	1.96%	<b>7.60%</b>	<b>1.80%</b>	22.95%	3.48%
List $\infty$	7.68%	1.97%	<b>7.61%</b>	<b>1.80%</b>	22.90%	3.41%
<b>Event Log with 5000 Traces</b>						
Set 1	<b>5.78%</b>	<b>1.87%</b>	7.42%	2.14%	9.98%	2.33%
Set $\infty$	<b>5.07%</b>	<b>1.13%</b>	6.68%	1.37%	9.82%	2.37%
List $\infty$	<b>5.08%</b>	<b>1.13%</b>	6.69%	1.38%	9.13%	2.27%

# Conclusions and future work

## Conclusions

We present a new prediction approach which:

- Extracts a transition system from the event log
- Enriches the transition system with machine learning models (Naïve Bayes + SVR)
- Exploits additional data attributes
- Better predictions with a real-life case study

## Future work

- Hyperparameters autotuning
- Simplify the usage for non-expert users
- Prediction with non-fitting traces

## **Chapter 2**

### Online mining of event streams

# Typical Event Log

Event #	Activity	Orig.	Time	...
<b>Case Id: <math>C_1</math></b>				
1	A	$U_1$	2014-01-01	...
2	B	$U_1$	2014-01-02	...
3	C	$U_2$	2014-01-03	...
4	E	$U_2$	2014-01-04	...
<b>Case Id: <math>C_2</math></b>				
1	A	$U_1$	2014-01-02	...
2	B	$U_1$	2014-01-03	...
3	D	$U_3$	2014-01-04	...
4	E	$U_3$	2014-01-05	...



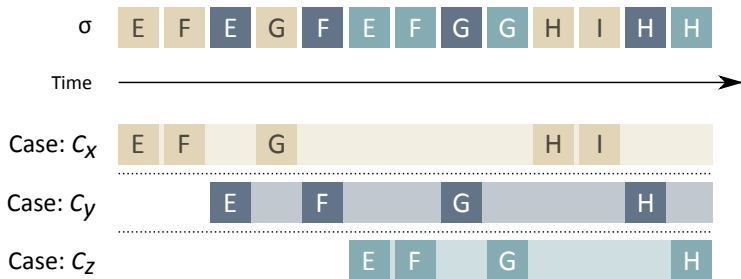
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4	E	$U_2$	2014-01-04	...
<b>Case Id: <math>C_2</math></b>				
1	A	$U_1$	2014-01-02	...
2	B	$U_1$	2014-01-03	...
3	D	$U_3$	2014-01-04	...
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Event #	Case Id	Activity	Orig.	Time	...
1	$C_1$	A	$U_1$	2014-01-01	...
2	$C_2$	A	$U_1$	2014-01-02	...
3	$C_1$	B	$U_1$	2014-01-02	...
4	$C_2$	B	$U_1$	2014-01-03	...
5	$C_1$	C	$U_2$	2014-01-03	...
6	$C_1$	E	$U_2$	2014-01-04	...
7	$C_2$	D	$U_3$	2014-01-04	...
8	$C_2$	E	$U_3$	2014-01-05	...

# Event Stream

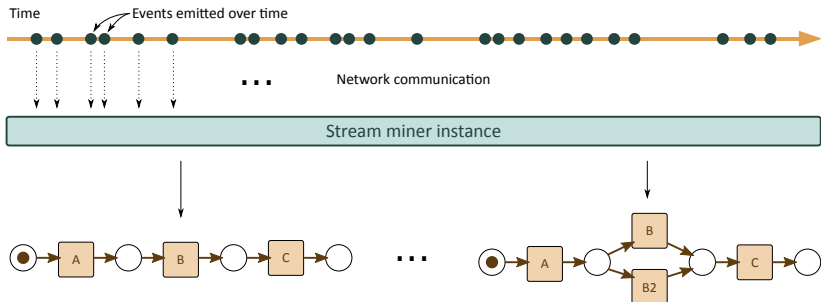
Representation of an event stream  $\sigma$ :



Boxes represent events

- Background colors represent the case id
- Letters inside are the activity names

# Streaming Process Discovery



The **stream miner** continuously receives **events** and, using the latest observations, updates the process model (e.g., a Petri Net)

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2. **Backtracking not feasible** over streams (algorithms required to make one pass over data → scale linearly w.r.t. the number of processed items)
3. The approach must deal with **variable system conditions**, such as fluctuating stream rates
4. It is important to quickly **adapt** the model to cope with unusual data values (concept drifts)



# Heuristics Miner

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Our approaches are based on Heuristics Miner, quite old ( $\sim$  2003) but still one of the most used algorithm

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Fundamental metric is “*dependency measure*” between two activities (e.g.  $a$ ,  $b$ ):

$$a \Rightarrow b = \frac{|a > b| - |b > a|}{|a > b| + |b > a| + 1} \in [-1, 1]$$

Where:

- $|a > b|$  is the number of times that  $a > b$  holds in the log
- $a > b$  holds if  $a$  executed at time  $t$  and  $b$  at  $t + 1$

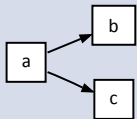
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If both  $a \Rightarrow b > \tau_{\text{dep}}$  and  $a \Rightarrow c > \tau_{\text{dep}}$  then:



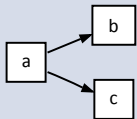
Relation ambiguity between  $b$  and  $c$ :

- XOR: either  $b$  or  $c$  is executed
- AND: both  $b$  and  $c$  are executed

# Heuristics Miner (cont.)

Given the dependency measure for all activity pairs and a threshold  $\tau_{\text{dep}}$ , the algorithm builds a directed dependency graph

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Relation ambiguity between  $b$  and  $c$ :

- XOR: either  $b$  or  $c$  is executed
- AND: both  $b$  and  $c$  are executed

Heuristics Miner proposes the “AND-measure”

$$a \Rightarrow (b \wedge c) = \frac{|b > c| + |c > b|}{|a > b| + |a > c| + 1} \in [0, 1]$$

If  $a \Rightarrow (b \wedge c) > \tau_{\text{and}}$  then AND relation, XOR otherwise

# Direct Following Matrix

Basic data structure for HM is **Direct Following Matrix**

## Direct Following Matrix

Given activities  $A, B, C, D$  and a log  $L$ ,  $|a > b|$  is the number of times that  $a$  is directly followed by  $b$  (within the same process instance) in the log  $L$

	$A$	$B$	$C$	$D$
$A$	0	52	64	91
$B$	52	0	24	87
$C$	64	24	0	13
$D$	91	87	13	0

# Proposed Approaches

## Our Proposal

We present three approaches, based on Heuristics Miner, for process discovery from event streams:

- (SW) Heuristics Miner with Sliding Window (*as baseline*)
- (LC) Heuristics Miner with Lossy Counting
- (LCB) Heuristics Miner with Lossy Counting with Budget

# Proposed Approaches

## Our Proposal

We present three approaches, based on Heuristics Miner, for process discovery from event streams:

- (SW) Heuristics Miner with Sliding Window (*as baseline*)
- (LC) Heuristics Miner with Lossy Counting
- (LCB) Heuristics Miner with Lossy Counting with Budget

## Fundamental Principle

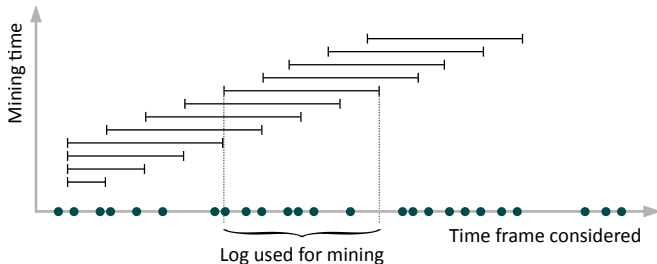
Recent observations are more important than older ones



# Heuristics Miner with SW

Basic idea is to iterate these steps

1. Collect events for a given time span
2. Generate a finite event log
3. Apply the “offline version” of the algorithm



# Frequency Counting with Lossy Counting

Given

- Max approximation error  $\epsilon$
- Variables: **A**, **B**, **C**
- *Bucket* size is  $w = \lceil \frac{1}{\epsilon} \rceil$
- $b_{current} = \lceil \frac{\text{no. of observed items}}{w} \rceil$

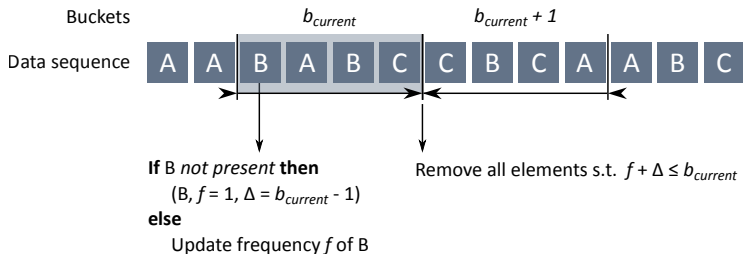
Lossy Counting uses a data structure  $\mathcal{D} = \{(\text{var}, \text{freq}, \text{max error})\}$

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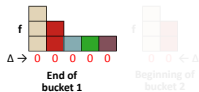
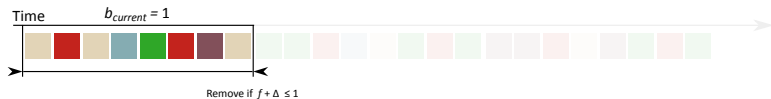
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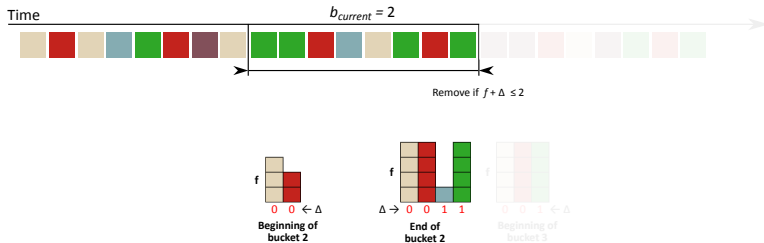
# LC/LCB Demo

## Lossy Counting Demo



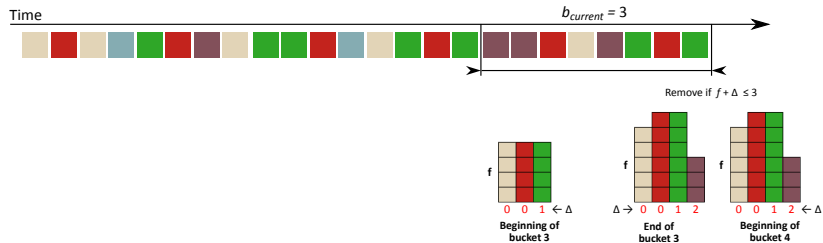
# LC/LCB Demo

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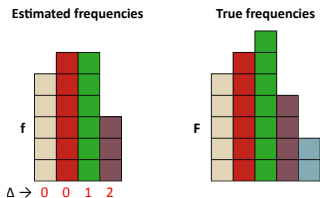
# LC/LCB Demo

## Lossy Counting Demo



# LC/LCB Demo

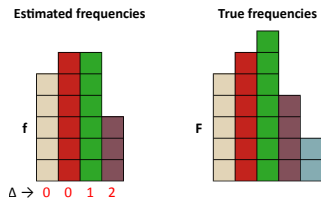
Comparison between Lossy Counting frequencies and true frequencies



These inequalities hold:  $f \leq F \leq f + \Delta \leq f + \epsilon N$

# LC/LCB Demo

Comparison between Lossy Counting frequencies and true frequencies



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Lossy Counting with Budget Idea

New bucket when there is no more space, then  $\epsilon = \frac{1}{\text{bucket size}}$



# Adaptation of LC/LCB to HM

To count direct following relations we need

- $\mathcal{D}_{\text{rel}}$  Actual relations frequencies, tuples:  $(a_s, a_t, f, \Delta)$
- $\mathcal{D}_{\text{act}}$  Latest activity names, tuples:  $(a, f, \Delta)$
- $\mathcal{D}_{\text{cases}}$  Latest activity of a case, tuples:  $(c, a, f, \Delta)$

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- Activities from  $\mathcal{D}_{\text{act}}$
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Actually, we show that updates on  $\mathcal{D}$  data structures affect only local parts of the model (incremental update of the process model)

# Evaluation Datasets

Artificial dataset characteristics:

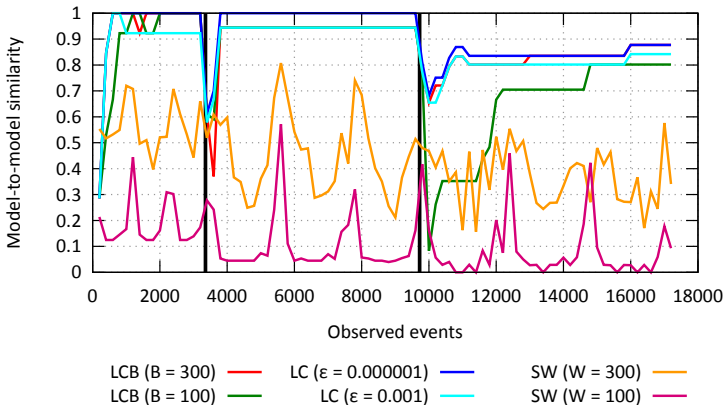
- Three randomly generated processes (to simulate concept drifts)
- Most complex model has 3 splits (1 AND and 2 XOR)
- Longest process has 16 activities
- Stream with 17 265 events

Real-world dataset (BPI Challenge 2012 log) characteristics

- Dutch Financial Institute
- 36 activities
- 262 198 events, among 13 087 process instances

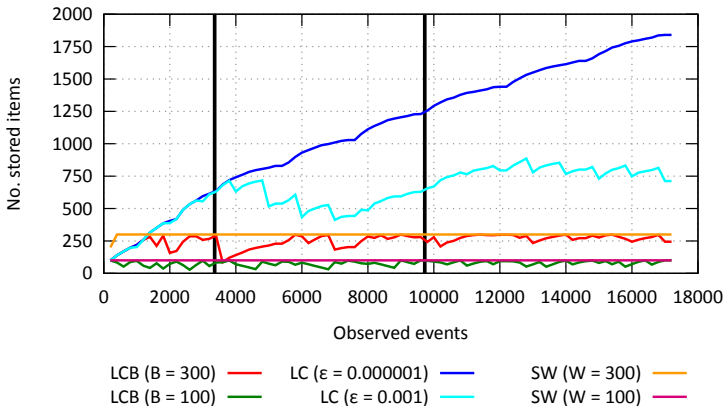
# Evaluation on Artificial Dataset

Assess the correspondence between original and discovered model



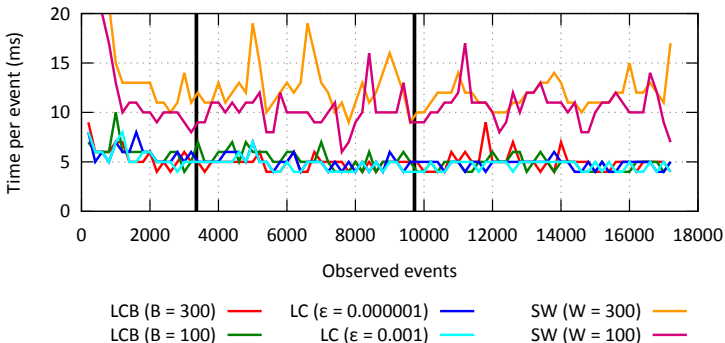
# Evaluation on Artificial Dataset

Space expressed as number of stored items



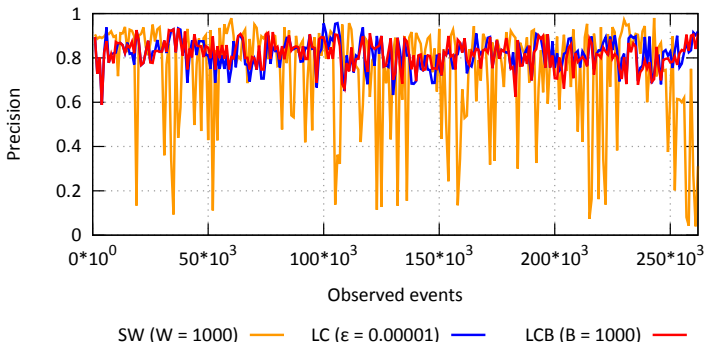
# Evaluation on Artificial Dataset

Time required to process each event



# Evaluation on BPI Challenge 2012

Precision of the discovered models



Time required to process an event:

**SW:** 24.59ms    **LC:** 5.68ms    **LCB:** 2.56ms



# Conclusions and Future Work

## Conclusions

- We discover process models from event streams
- Three approaches proposed, based on Heuristics Miner (with Sliding Window, with Lossy Counting, and with Lossy Counting with Budget)
- Experimental results on both artificial and real dataset, with improvements in terms of quality of the mined models, execution time, and space requirements as well

## Future Work

- Improve the process analyst to mine different perspectives
- Animations to point out process drifts locations

# With respect to KAOS...

We can model the prediction problem as a stream-based approach:

- Prediction model based on a-priori knowledge
- Prediction model could be online adapted to deal with concept drifts
- Predictions asked in real time